

HOMEWORK 8

Problem 1. §4.3 #13

Problem 2. §5.1 #1(c)(d)

Problem 3. For each pair of vectors, find the scalar projection of \mathbf{v} onto \mathbf{w} as well as the vector projection of \mathbf{v} onto \mathbf{w} .

$$\begin{aligned} \text{(a) } \mathbf{v} &= \begin{bmatrix} 6 \\ 0 \\ 0 \end{bmatrix} & \mathbf{w} &= \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} . \\ \text{(b) } \mathbf{v} &= \begin{bmatrix} 6 \\ 0 \\ 0 \end{bmatrix} & \mathbf{w} &= \begin{bmatrix} 6 \\ 0 \\ 8 \end{bmatrix} . \\ \text{(c) } \mathbf{v} &= \begin{bmatrix} 12 \\ 0 \\ 0 \end{bmatrix} & \mathbf{w} &= \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} . \end{aligned}$$

Problem 4. §5.2 #1(b)(c) Beware: $R(A)$ is the *column space* of A . (The R stands for range.) I'll try to stick with $\text{row}(A)$ and $\text{col}(A)$.

Problem 5. §5.2 #8

Problem 6. For each of the following systems $A\mathbf{x} = \mathbf{b}$, find all least squares solutions.

$$\begin{aligned} \text{(a) } A &= \begin{bmatrix} 1 & 1 & 2 \\ 2 & 0 & 2 \\ 1 & 0 & 1 \\ 1 & 1 & 2 \end{bmatrix}, & \mathbf{b} &= \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} . \\ \text{(b) } A &= \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, & \mathbf{b} &= \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} . \end{aligned}$$