MATH 362 - ADVANCED CALCULUS II Projects

- 1. Peano curve: a space filling curve. See exercise 31 in p.94 in Rosenlicht, and section 9.3 p.407 in Strichartz. Bob Cordwell.
- 2. Show that in finite dimensional vector spaces, all norms are equivalent. Need some linear algebra, see exercises 22 and 23 p. 93 in Rosenlicht.
- **3.** Equicontinuity and Arzela-Ascoli Theorem. See Sec 7.6 p.309 and exercise 10 in section 9.2 in Strichartz.
- 4. The contraction mapping theorem or fixed point theorem. Applications (Newton's method, how to compute the square root of a number?). Rosenlicht Section 7.1, Strichartz Section 9.3.4 p.397. T. J. Middleton and Jeniffer Campbell.
- 5. Approximation by polynomials: best approximation by n degree polynomials, Chebychev polynomials and applications to engineering. In *Real analysis with Real Applications* by K. R. Davidson and A. P. Donsig, Sections 10.5, 10.6 and 10.7. Robert Seletsky, Wei Lui and Sezi Bakim.
- **6.** Approximation by polynomials: splines and uniform approximation. Applications to engineering. In *Real analysis with Real Applications* by K. R. Davidson and A. P. Donsig, Sections 10.8, 10.9. **Bill Young and Carlos Gallegos.**
- 7. Convexity and optimization. In *Real analysis with Real Applications* by K. R. Davidson and A. P. Donsig, Chapter 16. **Peter Al-Hokayem.**
- 8. Rearrangements for conditionally or absolutely convergent series. Strichartz Section 7.2.2 p.256, Rosenlicht, Section 7.2, p. 146-149 and exercise 14 in p. 162. **Danielle Kellerup.**
- **9.** The fundamental theorem of algebra, an analytic proof. Rosenlicht exercise 34, p. 165; will need exercise 32 p. 164 or exercise 17 in p. 162. **Bryan Price.**

For the last projects I can give you hand outs to guide you. You can work on your own, or in a team. I would like a paper of no more than 5 pages per person in the team. It will be ideal if you agreed to make a short presentation in class so that all of you can learn what each of you is working on. You could propose a project not listed, but you should talk to me about it.